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The formation of spiral galaxies: adiabatic compression with Young’s algorithm and the relation of dark matter haloes to their primordial antecedents

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ABSTRACT

We utilize Young’s algorithm to model the adiabatic compression of the dark matter haloes of galaxies in the THINGS survey to determine the relationship between the halo fit to the rotation curve and the corresponding primordial halo prior to compression. Young’s algorithm conserves radial action and angular momentum, resulting in less halo compression than more widely utilized approximations. We find that estimates of the parameters of NFW haloes fit to the current dark matter distribution systematically overestimate the concentration and underestimate the virial velocity of the corresponding primordial halo. It is the latter that is predicted by dark matter simulations; so accounting for compression is a necessary step for evaluating whether massive galaxies are consistent with dark matter-only simulations. The inferred primordial haloes broadly follow the $c-V_{200}$ relation expected in a Λ cold dark matter (Λ CDM) cosmogony, but often scatter to lower concentrations. We are unable to obtain fits at all for those galaxies whose current dark matter haloes are poorly described by the NFW form. We thus find a mixed bag: some galaxies are reasonably well described by adiabatic compression within a primordial NFW halo, while others require an additional mechanism that reduces the density of dark matter below the primordial initial condition.

Key words: galaxies: evolution – galaxies: formation – galaxies: haloes – galaxies: spiral – galaxies: structure.

1 INTRODUCTION

In the early Universe, the dark matter and baryons are well mixed (Spergel et al. 2003). However, as the baryons cool and dissipate energy, they fall to the centre of the dark matter haloes and form the various types of galaxies (White & Rees 1978; Fall & Efstathiou 1980; Gunn 1982). The dark matter halo responds gravitationally to the infall and settling of baryons by compressing. Initially considered as an adiabatic process in an isolated dark matter halo, this same process also pertains in the context of the modern hierarchical picture of galaxy formation (Choi et al. 2006). The compression of dark matter haloes by baryonic infall is an inevitable consequence of the rearrangement of mass necessary to form a galaxy. It distorts the initial NFW density profiles predicted by cosmological structure

formation simulations (Navarro, Frenk, & White 1997) to a form that lacks an analytical description.

The Blumenthal method (Blumenthal et al. 1986) has been the standard in the literature since its initial development; however, multiple groups have shown that this formalism tends to overpredict the compression of the halo (e.g. Barnes 1987; Sellwood 1999; Gnedin et al. 2004). The drawback of this method is that it assumes all particles in the halo are on circular orbits (which is equivalent to assuming that the radial action of all such particles is zero). Historical examples of computing adiabatic compression exactly have required computationally expensive hydrodynamic simulations of cooling gas (Gottloeber et al. 2002; Abadi et al. 2003; Governato et al. 2004). However, Young (1980) developed a method to compute the adiabatic compression of spherical systems exactly by also accounting for random motions of particles in the halo (thus conserving the radial action in addition to the angular momentum). This method was first applied to the compression of dark matter

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haloes by Wilson (2004) and Sellwood & McGaugh (2005). Disc galaxies are not spherical, but the monopole term dominates so that Young’s method is as accurate as the equivalent (and computationally far more expensive) fully hydrodynamic simulation (Sellwood & McGaugh 2005).

The Blumenthal adiabatic contraction method predicts steeper inner profiles for initially NFW haloes than observed, which led Dutton et al. (2013) to suggest that haloes remain uncontracted or even expand slightly during galaxy formation. Adiabatic contraction cannot simply be switched off, so some additional mechanism must be invoked to mitigate its effects. A partial solution may be offered by light-weight IMFs; by reducing the mass in stars we can reduce the amount of compression they induce. However, the small scatter in the Tully–Fisher relation precludes arbitrary adjustment of the IMF, while its normalization is consistent with high surface brightness discs being nearly maximal (McGaugh 2005b) like the Milky Way (Flynn et al. 2006; Bovy & Rix 2013). Because Young’s algorithm correctly predicts less contraction than the Blumenthal algorithm, it allows for an IMF that is heavy enough to be consistent with these results.

Adiabatic contraction is not the only process to dynamically shape the dark matter halo of a galaxy. Feedback driven outflows (Navarro, Eke, & Frenk 1996; Read & Gilmore 2005; Pontzen & Governato 2012) and dynamical friction (El-Zant, Shlosman, & Hoffman 2001; Weinberg & Katz 2002; Johansson, Naab, & Ostriker 2009) can in principle counteract the compression of the halo. However, Sellwood (2008) have shown that the bar-halo friction proposed by Weinberg & Katz (2002) cannot cause a significant reduction in density (see also McMillan & Dehnen 2005). The mechanism described by El-Zant et al. (2001) likely results in an insignificant density reduction due to a number of issues described by Jarrel & Sellwood (2009), and an extremely massive satellite (~ 1 per cent of the virial mass of the halo) would have to sink in the galactic potential in order to cause a significant density reduction (Sellwood 2013). The magnitude we infer for such mechanisms as feedback driven outflows and dynamical friction depends on the amount of adiabatic contraction that occurs in the first place. In order to constrain the strength of feedback mechanisms, one must first correctly model the compression.

Here, we extend the study of Sellwood & McGaugh (2005) by applying Young’s algorithm to a sample of galaxies from the THINGS (de Blok et al. 2008; Walter et al. 2008) survey and look to relate the observed properties of galaxies with the characteristics of the primordial halo. In Section 2, we present our results in applying the algorithm to galaxies from the THINGS survey. In Section 3, we develop an analytical method for relating observed parameters of spiral galaxies to their primordial NFW halo and compare the predictions with observational constraints from lensing surveys. In Section 4, we summarize our conclusions.

2 DATA AND ANALYSIS

2.1 The THINGS sample

We adopt as our sample the THINGS galaxies analysed by de Blok et al. (2008). This provides a sample of well-resolved disc and gas-rich dwarf galaxies with observations of both stars and gas, both of which are essential to proper mass modelling. The stellar mass model is provided by *Spitzer* 3.6 μ observations while the atomic gas content has been observed with the VLA (Walter et al. 2008).

de Blok et al. (2008) fit NFW models to the data for definite prescriptions for the stellar mass-to-light ratio provided by population

synthesis models. These fits to the *current* distribution of dark matter provide a reference point for interpreting the effects of adiabatic contraction. In effect, we obtain the ‘before and after’ picture of the dark matter distribution given the assumption of a primordial NFW halo that has adiabatically contracted under the influence of the observed distribution of stars and gas.

As discussed above, these assumptions provide a vital starting point for relating the results of structure formation simulations with real observed galaxies. These assumptions may not be sufficient in all cases. It is therefore important to understand what we do not fit as well as what we do fit.

We have applied Young’s method to 12 of the 17 galaxies modelled by de Blok et al. (2008). Of the 12 galaxies modelled, the fits found are generally acceptable, modulo the expected minor issues discussed in detail below. Of the five remaining galaxies, one is NGC 6946. This galaxy is rather face-on, and the resulting mass model is sensitive to debatable choices for the inclination. We therefore omit it from consideration.

Four galaxies, NGC 925, NGC 2366, NGC 2976, and IC 2574, cannot be fitted with an NFW halo. de Blok et al. (2008) find unphysically low concentrations for the current dark matter distribution. This is the classic sign of galaxies that suffer from the cuspcore problem (de Blok, McGaugh, & Rubin 2001; Kuzio de Naray, McGaugh, & de Blok 2008; Oh et al. 2011). Adiabatic contraction tends to increase the concentration of the primordial dark matter halo, so an unphysically low concentration in the *current* dark matter halo implies an antecedent *primordial* halo whose concentration is still less consistent with Λ cold dark matter (Λ CDM). These are galaxies for which feedback or some other mechanism must be invoked in order to rearrange the primordial halo mass distribution predicted by structure formation simulations.

Modelling feedback is beyond the scope of this paper, and the many attempts to do so are still far from satisfying observational requirements (McGaugh 2004). Rather than attempt to model every conceivable effect, our aim is to simplify the problem in order to gain physical insight into one basic process of galaxy formation. We focus on adiabatic contraction because we know that it is a physical effect that must be important, and which largely precedes any subsequent feedback from star formation or AGN in the condensed baryonic mass. It is necessary to get this step right before determining the magnitude of required feedback effects.

We should not read too much into the numbers of galaxies that can and cannot be fit. The THINGS project provides ideal data for our exercise. It includes a nice spectrum of disc galaxy properties, but it does not provide a complete sample that is representative of the numbers of galaxies at each property. We shall see that of the galaxies that can be fit, the inferred primordial haloes are often consistent with the concentration–virial mass relation predicted by Λ CDM. Sometimes the data fall to lower concentrations than expected, while it is rare for the inferred concentration to run high. Among the galaxies that we cannot fit, the concentrations are all too low. This is the general rule for low-mass and low surface brightness galaxies (de Blok 2010). This should be kept in mind when interpreting the distribution of fit parameters for those galaxies that can be fit.

2.2 Application of Young’s method

We assume that the primordial haloes exhibit spherical, NFW potentials of the form

$$\Phi_{\text{NFW}}(r) = -\frac{GM_s}{r_s} \frac{\ln(1 + (r/r_s))}{r/r_s}. \quad (1)$$

Here $M_s = 4\pi\rho_s r_s^3$ and $\rho_s = 4\rho(r_s)$. These can be related to the more frequently used concentration c , and virial velocity, V_{200} , by noting that $c = r_{200}/r_s$ and $V_{200} = 10cr_s H_0$.

The two-parameter NFW profile has been superseded by the three-parameter Einasto profile (Navarro et al. 2004; Merritt et al. 2005) in fitting simulated haloes (see Chemin, de Blok, & Mamon 2011 for Einasto fits to the THINGS sample). While we could implement an Einasto profile, we choose to use the NFW profile for several reasons. First, we wish to minimize the number of free parameters. Secondly, the difference between NFW and Einasto profiles is not observationally distinguishable (McGaugh et al. 2007), so there is no added value in attempting to make this distinction. Finally, the relation between NFW parameters and the parameters of the cosmology in which haloes form is well documented (McGaugh, Barker, & de Blok 2003; Macciò, Dutton, & van den Bosch 2008).

Even limiting ourselves to the two-parameter NFW model, we expect some degeneracy among our fit parameters. There is a strong degeneracy between stellar mass and halo parameters (Kent 1987) stemming from the fact that a single parameter suffices to describe rotation curve data (McGaugh 2004). Even with a fixed stellar mass as implemented here, NFW haloes are largely self-degenerate over the finite range of radii constrained by real observational data: one NFW model looks much like another at small radii even if they differ greatly at large radii. Nonetheless, we can explore $M_s - r_s$ space and obtain a best fit.

For each galaxy, we initially define a large range in M_s and r_s , and build a Monte Carlo grid to explore this parameter space. After these initial simulations, we further refine the grid about the best-fitting parameters to find the minimum χ^2 . In Fig. 1, we show an example of a contour plot for χ^2 of initial coarse grid in the $M_s - r_s$ parameter space of NGC 2403. The crescent shape in the $M_s - r_s$ parameter space is consistent for all galaxies in our sample, and is typical of the covariance of NFW fit parameters (de Blok et al. 2001).

We emphasize that the error bars on the rotation curves are only estimates of the true uncertainties which attempt to take into account error in the tilted ring fits, uncertainties in inclination, differences in the velocities of the approaching and receding sides of the galaxy

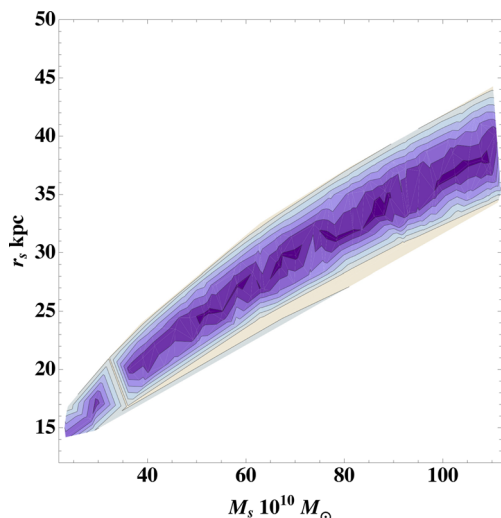


Figure 1. Example of the initial coarse grid for NGC 2403. Contours represent regions of constant χ^2 . The crescent shape of this parameter space is consistent over all galaxies.

as well as other effects (for a more detailed description of error bars, refer to de Blok et al. 2008). While this all-inclusive approach is likely an overestimate of the true error, the uncertainty in the assumption of IMF is likely to dominate over the uncertainties in the rotation curve. Thus the measured values of χ^2 are unlikely to be completely representative of the true accuracy of the fit and are rather used as mechanisms to fairly derive compressed halo fits in a comparable way to the uncompressed NFW haloes of de Blok et al. (2008).

The degree of compression of the primordial halo is directly related to the chosen stellar IMF. Unfortunately, the mass-to-light ratios for these galaxies are reasonably unconstrained. de Blok et al. (2008) provide three NFW fits using a diet-Salpeter IMF (a version of the Salpeter IMF scaled down in mass by 70 per cent to not exceed maximum disc as estimated by Bell & de Jong 2001), a Kroupa IMF (Kroupa 2001), and a free M_*/L (where the change in M_*/L as a function of radius is given by the colour gradient and the resulting stellar rotation curve is then scaled with a uniform constant). The Kroupa IMF has a flatter slope at $M < 0.5 M_\odot$ and so is less massive than the diet-Salpeter IMF. We therefore expect less compression when adopting the Kroupa IMF than with the diet-Salpeter IMF.

For our study, we have chosen to model all galaxies using the diet-Salpeter IMF, understanding that this may not represent the exact M_*/L for all galaxies in the THINGS survey. A Salpeter-like IMF is favoured in the spiral bulge models of Dutton et al. (2013) which serves as additional motivation for this choice of IMF. Furthermore, the choice of the diet-Salpeter IMF demonstrates how Young’s algorithm can work with a heavier IMF without overpredicting compression. We provide three examples of what we denote as ‘low concentration galaxies’ (LCGs), where the baryonic component is super-maximal for this choice of IMF, causing the NFW fit to have an extremely low concentration. We provide an additional fit for these three galaxies, assuming the Kroupa IMF¹ to demonstrate how the M_*/L can play a significant role in the rotation curve fit. One expects a fair amount of scatter in the relation between colour and mass-to-light ratio for any given IMF, so it is likely that the LCGs are simply galaxies that happen to scatter low in M_*/L rather than having intrinsically different IMFs. Nevertheless, one should bear in mind that the absolute normalization of the IMF is an irreducible systematic uncertainty in this (or any similar) exercise.

Table 1 lists the galaxies used in our study. This includes specific components for each model. Table 2 lists parameters for the LCGs which have been refitted using a Kroupa IMF. For the remainder of this section, we will refer to the uncompressed primordial dark matter halo as ‘PH’, the compressed dark matter halo as ‘CH’, and the NFW halo which de Blok et al. (2008) fit to each rotation curve as ‘dBH’.

2.3 Fits for individual galaxies

2.3.1 NGC 2403

NGC 2403 is a high surface brightness late-type Sc spiral galaxy. We have fit two models for this galaxy, the first assuming a one-component disc, and the second assuming an additional bulge component. Fig. 2 depicts the former while Fig. 3 depicts the latter.

¹ What Bell & de Jong (2001) call a Kroupa IMF does not include brown dwarfs. Including these, as would be appropriate here since we are concerned with the entire baryonic mass of the stellar disc, would result in a mass similar to the diet-Salpeter IMF. We maintain the distinction to illustrate the effects of the uncertainty in the IMF.

Table 1. *i.* M_*^B and $\Upsilon_{*,B}^{3.6}$ were left as free parameters and differ from predictions [see de Blok et al. (2008), table 4]. *ii.* The mass model neglects the colour gradient [see de Blok et al. (2008), table 4].

Galaxy (1)	$\log M_*^D$ (2)	$\Upsilon_{*,D}^{3.6}$ (3)	$\log M_*^B$ (4)	$\Upsilon_{*,B}^{3.6}$ (5)	de Blok parameters			This paper		
					c (6)	V_{200} (7)	χ_v^2 (8)	c (9)	V_{200} (10)	χ_v^2 (11)
NGC 2403 (1 comp)	9.71	0.41	9.9 ± 0.2	109.5 ± 1.0	0.55	6.2	134.9	0.64
NGC 2403 (2 comp)	9.67	0.39	8.63	0.60	9.8 ± 0.2	110.2 ± 1.0	0.56	6.1	140.0	0.68
NGC 2841	11.04	0.74	10.40	0.84	16.1 ± 0.2	183.2 ± 1.2	0.42	10.2	193.8	0.36
NGC 2903 (outer)	10.15	0.61	9.33	1.30	30.9 ± 0.6	112.9 ± 0.6	0.36	21.2	118.7	0.32
NGC 3031	10.84	0.80	10.11	1.00	3.0 ± 2.9	190.9 ± 161.1	4.36	2.4	187.6	4.40
NGC 3198 (1 comp)	10.40	0.80	7.5 ± 0.4	112.4 ± 2.1	1.37	3.5	129.4	1.83
NGC 3198 (2 comp)	10.45	0.80	9.46	0.73	5.1 ± 0.5	122.7 ± 4.9	2.88	3.1	147.0	2.94
NGC 3621	10.29	0.59	3.7 ± 0.2	165.5 ± 5.9	0.81	3.2	174.1	1.84
NGC 4736	10.27	0.63	9.59^i	0.33^i	11.4 ± 9.8	35.2 ± 0.3	1.51	7.6	39.8	1.74
DDO 154	7.42	0.32	4.4 ± 0.4	58.7 ± 4.3	0.82	4.5	72.4	1.11
NGC 7793	9.44	0.31	5.8 ± 1.4	156.6 ± 39.1	4.17	4.4	188.7	5.11
Low concentration galaxies										
NGC 3521	11.09	0.73	<0.1	403.2 ± 123.2	8.52	1.6	201.6	11.31
NGC 5055	11.09	0.79	9.32^{ii}	0.11^{ii}	<0.1	450.1 ± 32.4	10.31	1.6	163.6	15.20
NGC 7331 (const) ⁱⁱⁱ	11.22	0.70	10.24	1.00	<0.1	>500	4.08	1.5	217.3	4.64

Table 2. *i.* M_*^B and $\Upsilon_{*,B}^{3.6}$ were left as free parameters and differ from predictions [see de Blok et al. (2008) table 5]. *ii.* The mass model neglects the colour gradient [see de Blok et al. (2008), table 5].

Galaxy (1)	$\log M_*^D$ (2)	$\Upsilon_{*,D}^{3.6}$ (3)	$\log M_*^B$ (4)	$\Upsilon_{*,B}^{3.6}$ (5)	de Blok parameters			This paper		
					c (6)	V_{200} (7)	χ_v^2 (8)	c (9)	V_{200} (10)	χ_v^2 (11)
NGC 3521	10.94	0.52	8.9 ± 2.0	128.4 ± 16.4	5.55	3.8	102.1	5.27
NGC 5055	10.94	0.56	9.81^i	0.34^i	2.1 ± 0.4	217.8 ± 21.2	1.45	1.9	212.7	2.83
NGC 7331 (const) ⁱⁱ	11.07	0.50	10.09	0.71	4.9 ± 0.4	200.0 ± 10.7	0.24	3.7	210.9	0.30

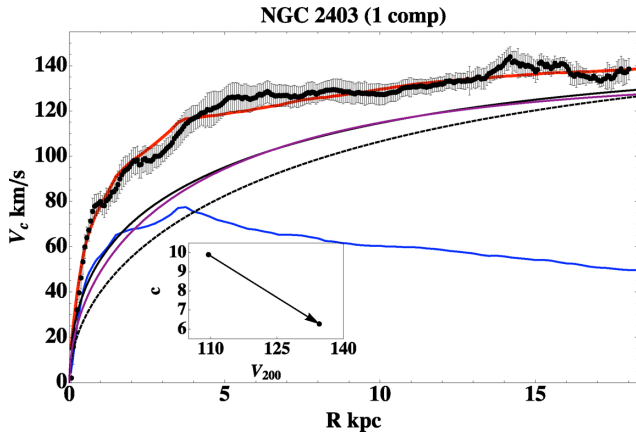


Figure 2. Rotation curve fit for NGC 2403 one-component model. The blue line represents the total baryonic component (stars + gas). The purple line shows the dBH. The dashed black line is the PH and the solid black line is the CH. Finally, the red line is the fit from summing the CH (solid, black) with the baryonic component (blue). This inset shows the best-fitting c and V_{200} for the dBH with an arrow pointing to the best-fitting parameters for the PH as calculated in this paper.

We can see that they are nearly identical. Our values for χ_v^2 for both CH fits are very comparable to the dBHs. As expected, our CHs have slightly more mass within ~ 4 kpc where the baryonic component of the rotation curve is approximately equal to that of

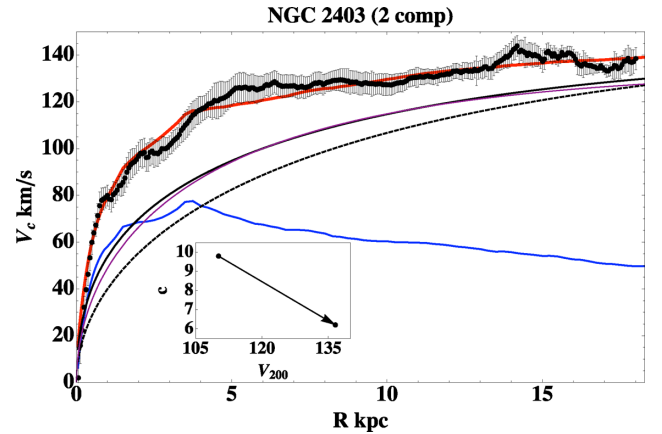


Figure 3. Rotation curve fit for NGC 2403 two-component model. Lines and inset are the same as in Fig. 2.

the dark matter. Our CH is indistinguishable from the dBH out to ~ 15 kpc where our CH continues to rise.

For the one-component disc model, our PH has a 23 per cent higher V_{200} than that of the dBH while the concentration has decreased by a factor of 64 per cent. Similarly, the PH of the two-component model has a V_{200} that is 23 per cent higher than that of the dBH while the concentration has decreased by a factor of 63 per cent.

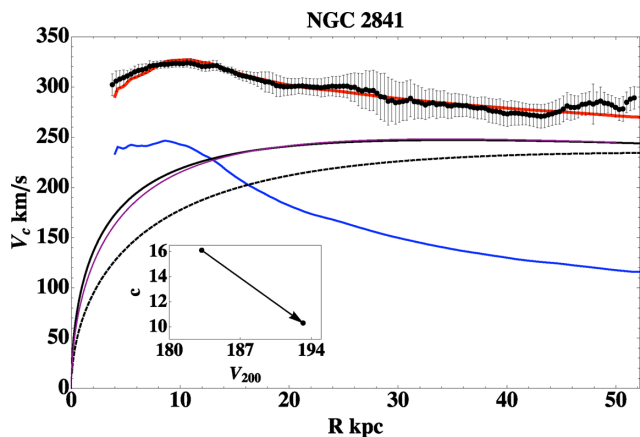


Figure 4. Rotation curve fit for NGC 2841. Lines and inset are the same as in Fig. 2.

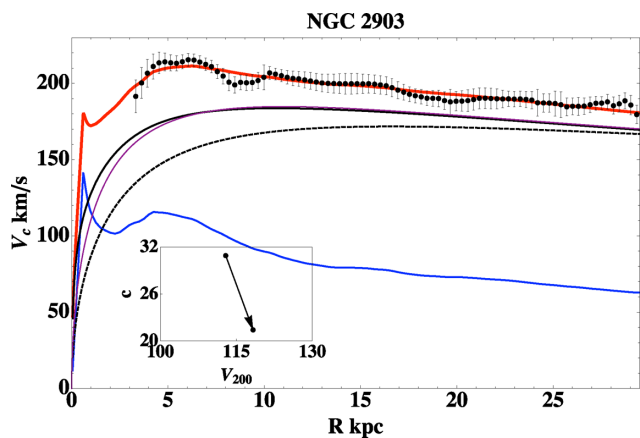


Figure 5. Rotation curve fit for NGC 2903. Lines and inset are the same as in Fig. 2. The innermost points have been omitted from the plot.

2.3.2 NGC 2841

NGC 2841 is an early-type (Sb) spiral galaxy. We use a two-component model to represent the bulge and disc; however the rotation curve data do not represent the inner 3 kpc. Our CH fits the rotation curve quite well (see Fig. 4). The CH is nearly identical to the dBH at all radii; however as expected, the CH has slightly more mass within ~ 13 kpc. The V_{200} of our PH is only 5.5 per cent larger than that of the dBH and the concentration has been reduced by a factor of 64 per cent.

2.3.3 NGC 2903

Here we only study the outer portion of the rotation curve of NGC 2903, an SBd galaxy, due to non-circular motions towards the centre. We use a two-component model to represent the bulge and disc and notice a slight decline in the rotation curve at large radii as well as an interesting feature around 10 kpc. This small jump is likely due to the tilted ring fit which demonstrates an abrupt shift in inclination at this radius. The inclination, however, is well behaved at all radii further out.

Our CH fits the rotation curve very well (see Fig. 5). Our fit is indistinguishable from the dBH for all radii greater than about 6 kpc, and again, the CH has slightly more mass in the inner parts. The V_{200} of our PH is only 5.1 per cent larger than that of the dBH and the concentration has been reduced by a factor of 61 per cent.

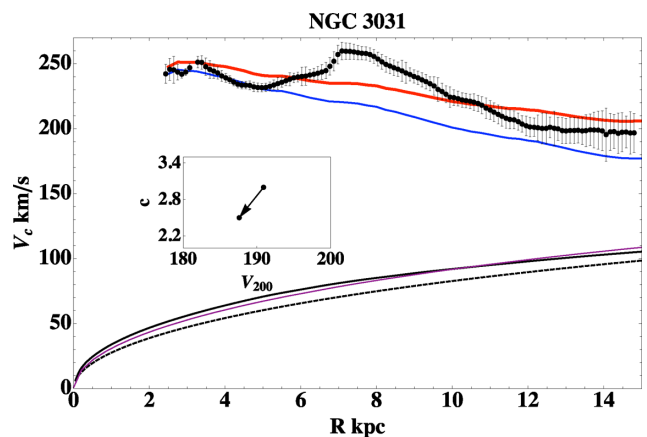


Figure 6. Rotation curve fit for NGC 3031. Lines and inset are the same as in Fig. 2.

2.3.4 NGC 3031

NGC 3031 is a grand design spiral galaxy. The baryonic contribution to the rotation curve is modelled by a two-component disc which is maximal. The baryonic component is completely dominant over the dark matter for all sampled radii. Features in the rotation curve, including the large bump spanning from $R = 6$ to 8 kpc, is likely due to an abrupt shift in inclination caused by non-uniform circular motion. The inclination increases steadily after this feature which might result in the decline in the rotation curve at large radii.

No smooth dark matter halo will be able to fit this rotation curve well due to the large bump at $6 < R < 8$ kpc because the baryonic component is not only dominant, but also smooth. Thus while our CH fit is comparable to the dBH, our χ^2 calculation arrives at this value by slightly overpredicting the inner and outer regions while underpredicting the aforementioned feature in the rotation curve (see Fig. 6).

2.3.5 NGC 3198

NGC 3198 is an SBc galaxy. Similar to NGC 2403, we study both a one- and two-component model for the disc. In both models, the baryonic component alone overpredicts the rotation curve at $R \sim 1$ kpc; however, this is less extreme in the one-component disc model. de Blok et al. (2008) note that there is evidence for the presence of a small bar which could affect the inner part of the rotation curve due to non-circular motions and cause the baryonic component to overpredict the rotation curve.

Our CHs fit the outer portions of the rotation curve well but the value for χ^2_v is plagued by the overprediction of the rotation curve by the baryonic component. Our fit for the two-component model is very comparable to the dBH for the same model with very slightly more mass at radii less than ~ 15 kpc. However, the CH model for one-component disc is not as good as the dBH, which has less mass at all radii out to $R \sim 30$ kpc (see Fig. 7 for the one-component model and Fig. 8 for the two-component model). Unlike NGC 2403, the one- and two-component models for NGC 3198 result are reasonably different PHs. For the one-component disc model, the V_{200} of our PH is 15.1 per cent larger than that of the dBH and the concentration has been reduced by a factor of 47 per cent. For the two-component disc model, the V_{200} of our PH is 19.8 per cent larger than that of the dBH and the concentration has been reduced by a factor of 61 per cent.

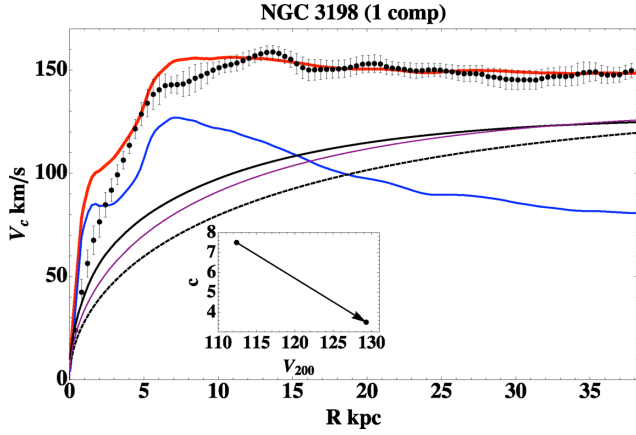


Figure 7. Rotation curve fit for NGC 3198 one-component model. Lines and inset are the same as in Fig. 2.

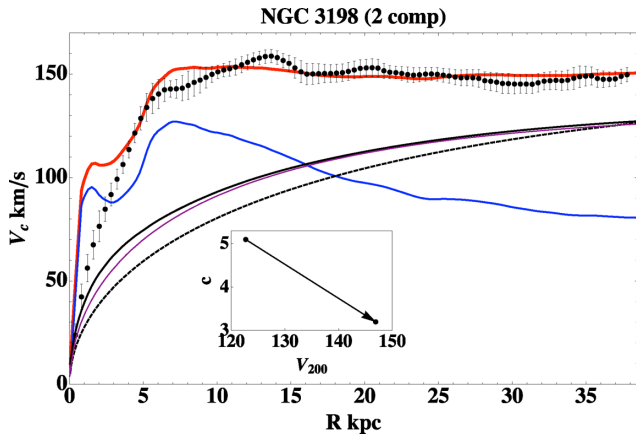


Figure 8. Rotation curve fit for NGC 3198 two-component model. Lines and inset are the same as in Fig. 2.

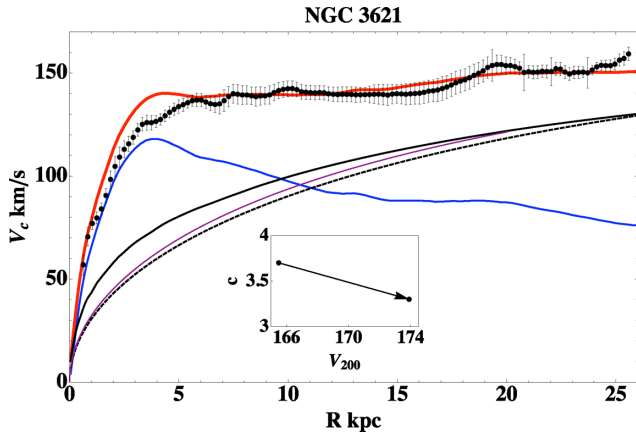


Figure 9. Rotation curve fit for NGC 3621. Lines and inset are the same as in Fig. 2.

2.3.6 NGC 3621

NGC 3621 is a late-type spiral galaxy. We use a one-component disc to model the stellar component and see that the baryonic component is nearly maximal. Our CH does well at $R > 7$ kpc, fitting V_{flat} almost perfectly (see Fig. 9). Despite this success, we find that our fit is not nearly as accurate as the dBH. Because the baryonic component is

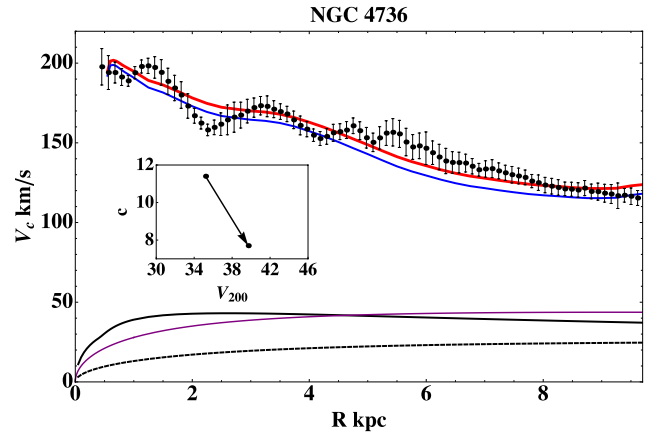


Figure 10. Rotation curve fit for NGC 4736. Lines and inset are the same as in Fig. 2.

nearly maximal at the inner radii, we find that in order to fit V_{flat} , we will overpredict the rotation curve at the inner radii. We can see that the CH has more mass than the dBH out to $R \sim 20$ kpc. We find that the V_{200} of our PH is only 5.2 per cent larger than that of the dBH and the concentration has been reduced by a factor of 14 per cent. This scenario is easily resolvable by choosing a lower M_*/L .

2.3.7 NGC 4736

NGC 4736 is one of the more unique galaxies in our sample, having a steeply declining rotation curve as well as a nearly maximum disc. We use a two-component model for the disc and scaled the mass of the bulge consistent with de Blok et al. (2008) so that the baryonic component would not be super-maximal. The rotation curve out to all radii sampled is already well described by the baryonic component with little need for dark matter. Furthermore, there are multiple features in the rotation curve and there is evidence of non-circular motion in the disc.

Because the rotation curve is so well described by the baryons, this galaxy has the least significant dark matter halo of all the galaxies in our sample. Despite this, our CH reveals a comparable fit to the dBH (see Fig. 10). The trend of a higher V_{200} and smaller concentration is also evident; however, there is much more freedom to choose halo parameters because the dark matter component is relatively insignificant for this galaxy.

2.3.8 DDO 154

DDO 154 is a prime example of a well-studied gas-rich dwarf galaxy. Because of its gas-rich nature, changes to M_*/L have little effect on the resulting best-fitting halo. We use a one-component disc and unlike NGC 4736, the dark matter component for this galaxy will dominate over the baryonic component for all radii.

Our CH does reasonably well fitting this galaxy (see Fig. 11). It is interesting to note that the CH has been overtaken by the PH at very small radii, unlike all other galaxies in our sample where this occurs at radii larger than what has been sampled. Because DDO 154 is so light, very little compression actually occurs. Our algorithm conserves mass by assuming that the PH is a well-mixed distribution of dark matter and baryons. In order to form the disc, the baryons are then removed from the PH, resulting in a CH that is simply the remnant of PH without the baryonic component. With this in mind, the V_{200} of the PH is 28.7 per cent larger than that of the dBH, while the concentration has remained reasonably unchanged.

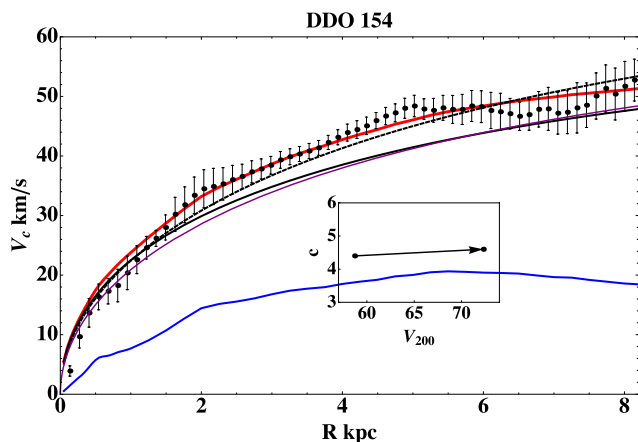


Figure 11. Rotation curve fit for DDO 154. Lines and inset are the same as in Fig. 2.

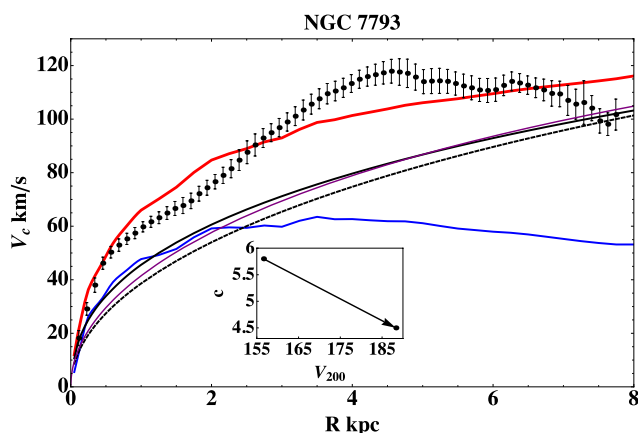


Figure 12. Rotation curve fit for NGC 7793. Lines and inset are the same as in Fig. 2.

2.3.9 NGC 7793

NGC 7793 is a late-type Sd spiral galaxy. We use a one-component model for the disc and note that the rotation curve begins declining at $R \sim 5$ kpc. The degree of this decline is relatively uncertain and varies for different studies of this rotation curve.

Because of the declining rotation curve and the necessity for a dark matter component comparable to baryonic component at the inner radii of this galaxy, any NFW halo and even more so, our CH, is doomed to failure for this galaxy. The χ^2 minimization algorithm will look to fit this galaxy by overpredicting the velocity at large radii and underpredicting the large bump at $3 < R < 5$ kpc and once again overpredicting the velocity at smaller R (see Fig. 12). The shape of the NFW halo is simply inconsistent with this galaxy. Our CH has more trouble because more mass is concentrated in the centre and we overpredict the rotation curve more than an ordinary NFW halo fit.

2.4 Low concentration galaxies

A clear trend among the fits thus far has been that the CH is more massive at the inner radii of the galaxies compared to the dBH. When the concentrations of the dBH approach zero, the compression of any PH will, by construction, provide a worse fit to the rotation curve. These types of galaxies often have super-maximal discs with

a baryonic component that declines below V_{flat} at smaller R . In other words, the dark matter component must be minimal in the inner portion of the galaxy as to not significantly overpredict the rotation curve, but increase steeply at larger R to make up for the decline in the baryonic component. A halo of this shape is inconsistent with the shapes of the compressed haloes derived in the previous subsection.

This problem is resolvable by decreasing M_*/L and we provide examples where adopting a Kroupa IMF over the diet-Salpeter IMF will allow for reasonable compression without an unrealistically low concentration. One might also note that Young's algorithm does not overpredict compression when a dominant baryonic component is present and therefore, the calculated compression for these galaxies is significantly different than what would be predicted using the Blumenthal method. For consistency, we do not include the fits to these galaxies in our further analysis of the nine galaxies in the previous subsection.

It must also be considered that although adopting a Kroupa IMF may allow for a better fit for a compressed halo, this does not necessarily rule out the choice of a diet-Salpeter IMF for a specific galaxy. There is an inherent scatter in M_*/L when adopting a diet-Salpeter IMF for a galaxy of a given colour (Bell & de Jong 2001). This scatter may cause the disc to become sub-maximal and thus potentially allowing for a reasonable fit using a compressed halo and a diet-Salpeter IMF. Hence, adopting a stellar IMF with a lower M_*/L is guaranteed to make the galaxy more susceptible to a compressed halo fit; however, it often cannot rule out a heavier IMF due to the inherent scatter in M_*/L . Indeed, the small scatter in the Tully–Fisher relation is predominantly attributable to scatter in the mass-to-light ratio, and precludes arbitrary variation of the IMF from galaxy to galaxy (Verheijen 2001; McGaugh 2005b). Here, we adopt a Kroupa IMF for the LCGs for the specificity in illustrating the effect of a different mass-to-light ratio.

2.4.1 NGC 3521

We use a one-component disc model to describe the stellar component of the rotation curve. The baryonic component rises slightly above observations from about $3 < R < 7$ kpc and then declines below observations at about $R > 8$ kpc, resulting in the necessity for a significant dark matter halo. In order to fit the outer portion of the rotation curve, we significantly overpredict the inner portion due to the strong compression from having a dominant baryonic component (see Fig. 13).

When adopting the Kroupa IMF, the disc is no longer super-maximal. Our CH differs significantly from the dBH, but is statistically a better fit (see Fig. 14). The dBH has a much higher V_{200} and concentration than the best-fitting PH. Neither fit is able to match the inner few data points leading to a higher χ^2_v than other galaxies in the sample; however, the CH fit does very well at about $R > 1.5$ kpc.

2.4.2 NGC 5055

NGC 5055 is an Sbc galaxy and we use a two-component disc to model the stellar contribution. The M_*/L for the bulge has been altered from what is predicted to match de Blok et al. (2008) and decrease the overprediction of the rotation curve at small radii. Despite this effort, the baryonic component still significantly overpredicts the rotation curve at about $4 < R < 12$ kpc. The baryonic component declines even more steeply than in NGC 3521, once again requiring a significant dark matter contribution at larger radii.

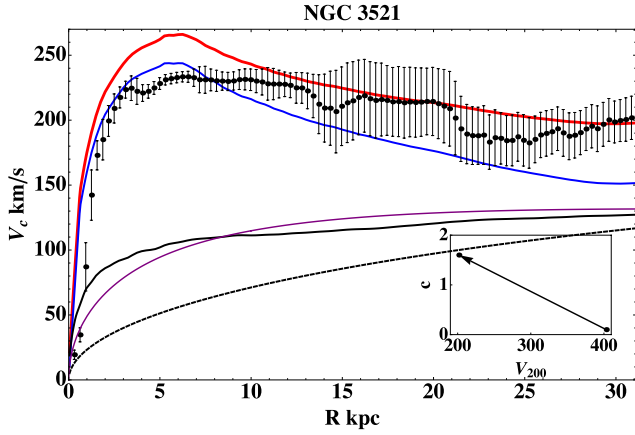


Figure 13. Rotation curve fit for NGC 3521. Lines and inset are the same as in Fig. 2.

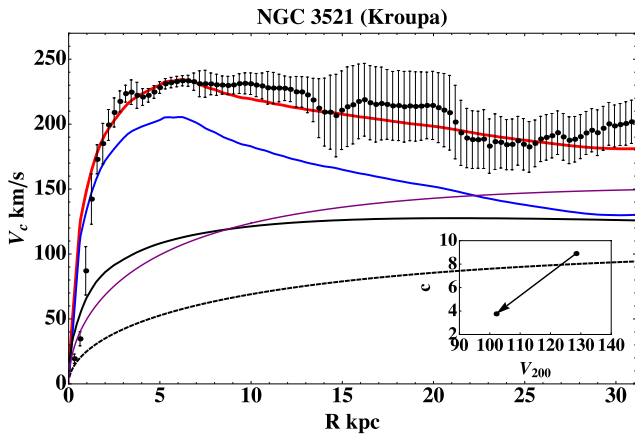


Figure 14. Rotation curve fit for NGC 3521 (Kroupa stellar IMF). Lines and inset are the same as in Fig. 2.

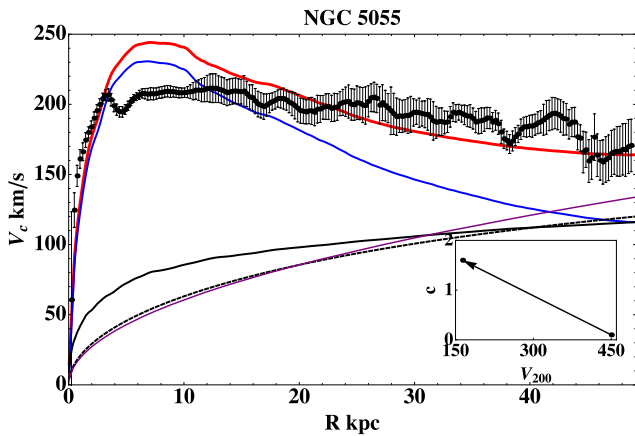


Figure 15. Rotation curve fit for NGC 5055. Lines and inset are the same as in Fig. 2.

In order to fit the outer portion of the rotation curve, we significantly overpredict the inner portion due to the strong compression from having a dominant baryonic component in the inner region (see Fig. 15).

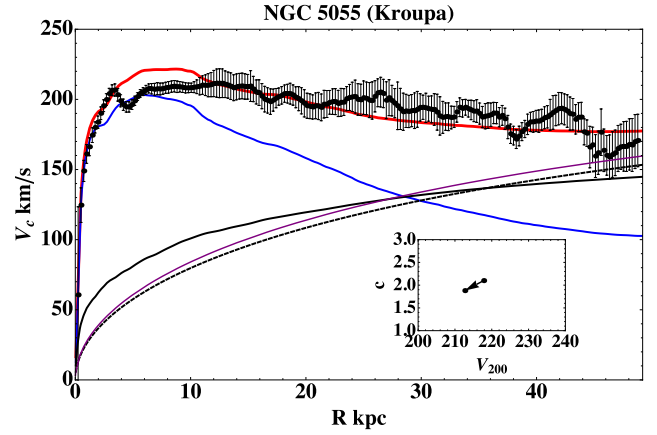


Figure 16. Rotation curve fit for NGC 5055 (Kroupa stellar IMF). Lines and inset are the same as in Fig. 2.

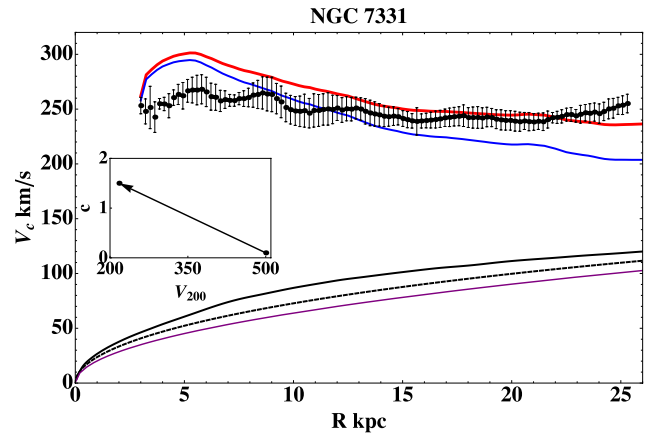


Figure 17. Rotation curve fit for NGC 7331. Lines and inset are the same as in Fig. 2.

When adopting the Kroupa IMF, the disc no longer overpredicts the rotation curve, but is maximal. Our CH does significantly worse than the dBH for this galaxy because of the presence of a significant decline in the baryonic component as well as a maximal disc (see Fig. 16). As was stated for the diet-Salpeter fit for this galaxy, in order to fit the outer portion of the rotation curve, we significantly overpredict the inner portion due to the strong compression from having a dominant baryonic component in the inner region.

2.4.3 NGC 7331

NGC 7331 is a early-type Sb spiral galaxy with a significant colour gradient. We use a two-component disc to model the stellar contribution. In order to be consistent with de Blok et al. (2008), we fit the rotation curve without a colour gradient due to the incompatibility of their mass models with the colour gradient (see Fig. 17). As is common among these LCGs, the baryonic component is super-maximal, and overpredicts the rotation curve at about $3 < R < 8$ kpc. Because there is only a shallow decline in the baryonic component, this galaxy requires respectively less dark matter than the other two in this subsection. Hence, our measure for χ^2_v is more comparable to that of the dBH.

When adopting the Kroupa IMF, the disc is no longer super-maximal and our CH provides a very good fit for this galaxy,

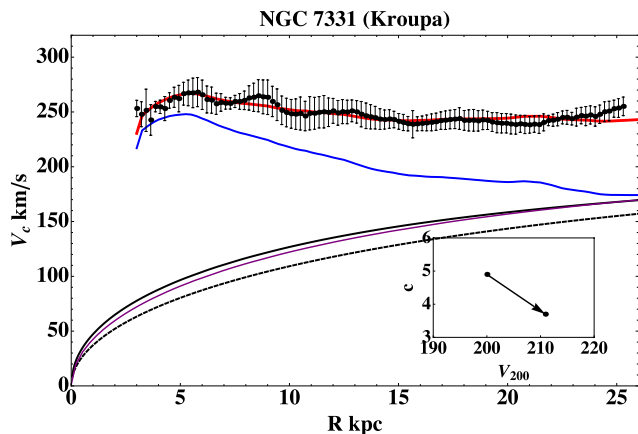


Figure 18. Rotation curve fit for NGC 7331 (Kroupa stellar IMF). Lines and inset are the same as in Fig. 2.

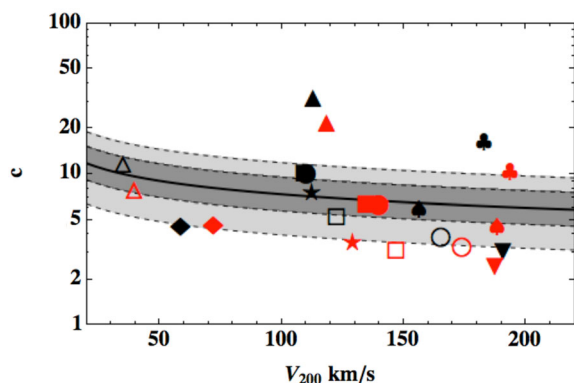


Figure 19. The c - V_{200} relationship for our primordial NFW haloes (red symbols) as well as for the de Blok et al. (2008) NFW haloes (black symbols). Corresponding symbols represent the same galaxy which can be identified in Table 1. The grey line represents the expected c - V_{200} relation from Λ CDM as derived in Macciò et al. (2008).

comparable to the dBH (see Fig. 18). Despite the disc being nearly maximal for this galaxy, the baryonic contribution to the rotation curve declines slowly; thus requiring a less dominant dark matter component at outer radii. Contrary to NGC 5055, the nearly maximal disc does not over compress the dark matter at the inner regions, allowing for a very good fit.

3 DISCUSSION

Having accurately computed halo compression for multiple different types of galaxies, we now aim to connect the observed properties of these galaxies with their host dark matter halo; bridging the gap between dark matter N -body simulations and disc galaxy formation. In Fig. 19 we plot the NFW halo parameters from the de Blok et al. (2008) NFW halo fits along with the parameters of the primordial haloes from our fits and compare with predictions from Λ CDM (Macciò et al. 2008). The halo parameters derived from our compression algorithm broadly agree with the $c - V_{200}$ relation predicted by Λ CDM, though more galaxies lie on the low-concentration side of the relation. We note that the NFW halo fits from de Blok et al. (2008) also tend to agree with the $c - V_{200}$ relation predicted by Λ CDM. Since the primordial NFW haloes parameters calculated from our compression algorithm tend to lie at the lower end of the

concentration region predicted by Λ CDM, one may argue that this work may favour the notion that actual haloes either exhibit no compression or possibly mild expansion. This statement is restricted to the galaxies we have been able to fit here, and does not address the broader problem of Λ CDM overpredicting the mass in the centres of low-mass and low surface brightness galaxies (Kuzio de Naray, McGaugh, & de Blok 2008; Kuzio de Naray, McGaugh, & Mihos 2009; de Blok 2010). There are galaxies within the THINGS sample that we were unable to fit with our compression algorithm which are likewise inconsistent with an ordinary NFW halo fit as well (these include NGC 925, NGC 2366, NGC 2976, and IC 2574). Competing effects such as dynamical friction and outflows counteract compression and both processes likely affect real galaxies. In low surface brightness galaxies in particular, the density profile requires halo expansion (Oh et al. 2011). However, there are certainly cases in our small sample where the primordial halo parameters derived from our compression algorithm agrees with the c - V_{200} relation predicted by Λ CDM better than the current NFW halo fit. This suggests that compression may be the dominant effect in higher mass galaxies, but it may be that there is no unique approach to modelling the density profile.

The general trend is that compression leads primordial haloes to have a higher V_{200} and lower concentration than what is inferred from directly fitting an NFW halo to the rotation curve. Estimates of these parameters by directly fitting NFW haloes will systematically overestimate the true concentration and underestimate the true virial velocity of the primordial halo as predicted by dark matter simulations.

We can use the apparent relation between compression and mass (Fig. 20) to prescribe an analytic method to map from a directly fitted NFW halo to the corresponding primordial halo. One simply fits the rotation curve with an NFW halo and uses the following relations to map the direct fit NFW halo parameters to the primordial NFW halo parameters:

$$V_{200,\text{prim}}(M_b) = \frac{V_{200,\text{fit}}}{A_V + B_V \log(M)} \quad (2)$$

$$c_{\text{prim}}(M_b) = c_{\text{fit}}(A_c + B_c \log(M)), \quad (3)$$

where M is either M_b or M_* (The fit constants take different values when choosing M_b or M_*).

In Fig. 20, we plot the ratios of our primordial halo NFW halo parameters with the best fit de Blok et al. (2008) parameters against the baryonic mass and stellar mass to determine the constants in these equations. We find: $A_V = 0.145$, $B_V = 0.072$, $A_c = 2.047$ and $B_c = -0.134$ when relating to M_b and $A_V = 0.417$, $B_V = 0.047$, $A_c = 1.762$ and $B_c = -0.109$ when relating to M_* . We emphasize that there is significant error associated with these values due to our small sample of galaxies as well as scatter in the data. The V_{200} relation exhibits a much tighter trend compared with the concentration relation where there is substantial scatter. There is also a large gap between most galaxies in our sample at the higher mass end and the sole galaxy, DDO 154, in the low-mass regime. In order to further constrain the fit constants, future studies would need to fill this gap.

This relation can also be used to relate haloes produced in simulations to a galaxy it will likely contain. Simply reverse the relation by inputting the primordial halo parameters and assuming that $M_b = f_b f_d M_{200}$, where f_b is the cosmic baryon fraction, M_{200} is the mass of the halo, and f_d is the fraction of the baryons that contribute

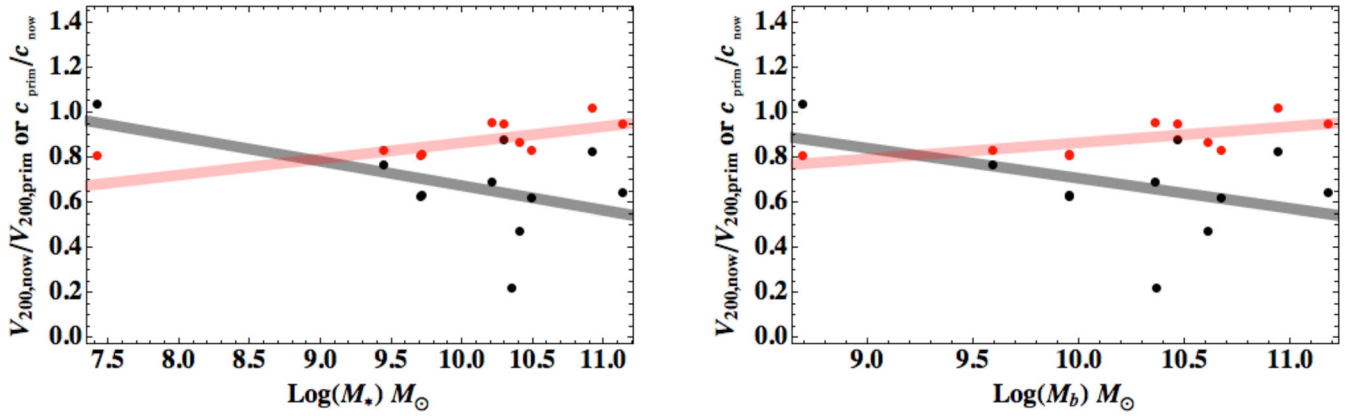


Figure 20. Left: ratios of our primordial NFW parameters with the de Blok et al. (2008) NFW halo parameters compared to the stellar mass of the galaxy. Right: ratios of our primordial NFW parameters with the de Blok et al. (2008) NFW halo parameters compared to the baryonic mass (stars+gas) of the galaxy. In both plots, red points represent the $V_{200,\text{now}}/V_{200,\text{prim}}$ and black points represent $c_{\text{prim}}/c_{\text{now}}$. The red and black lines are the respective best fits. The data for NGC 4736 have been excluded for its vast inconsistency with the rest of the sample.

to the observed galaxy. Constraints from the baryonic Tully–Fisher relation (BTFR) (McGaugh 2012) suggest² that:

$$\log(f_d) = \log\left(\frac{f_v^3 V_f}{100 \text{ km s}^{-1}}\right) - 1 \quad (4)$$

where $f_v = \frac{V_{\text{flat}}}{V_{\text{vir}}}$. The choice of f_v is not particularly obvious. Using $V_{2.2}$ rather than V_{flat} , Reyes et al. (2012) found $1 \leq f_v \leq 1.3$ for high-mass galaxies (which is similar to earlier studies by Eke et al. 2006 and Dutton et al. 2010); however there is substantial scatter around these values (see Fig. 22 for how this value relates to the stellar mass of the galaxy). It is quite possible that the relation between M_h and M_b is not one-to-one and thus there is some range in possible choices of f_d . This range must be modest in order to not induce a large amount of scatter in the Tully–Fisher relation, or there must be some fine-tuned covariance between f_d and other parameters (McGaugh et al. 2010).

Continuing with the idea of relating the primordial NFW parameters with properties of the constituent spiral galaxy, we compare our primordial halo parameters with observational constraints on the observed mass– V_{200} relation (OMVR) as well as the halo-to-stellar mass relation (HSMR) and the optical-to-velocity relation (OVVR) from Reyes et al. (2012) (see Figs 21–23). We can see in all three figures that our results are broadly consistent. However, there is considerable scatter, and important differences in detail.

Figs 21–23 show both the NFW fit to the current dark matter distribution (de Blok et al. 2008) and the primordial halo before compression. Reyes et al. (2012) employ a somewhat lighter IMF than we do here. This would place the corresponding primordial halo intermediate between our result and that of de Blok et al. (2008), which is the limit of no compression. The difference, while apparent, is modest. It cannot reconcile the discrepant cases that fall outside the band of Reyes et al. (2012). The effect is not large enough for individual galaxies, and a systematic change to the IMF would improve the agreement of some cases only at the expense of making those currently in good agreement worse. It is likely that the population models simply misestimate the mass-to-light ratio in some cases, but these are not necessarily the discrepant cases.

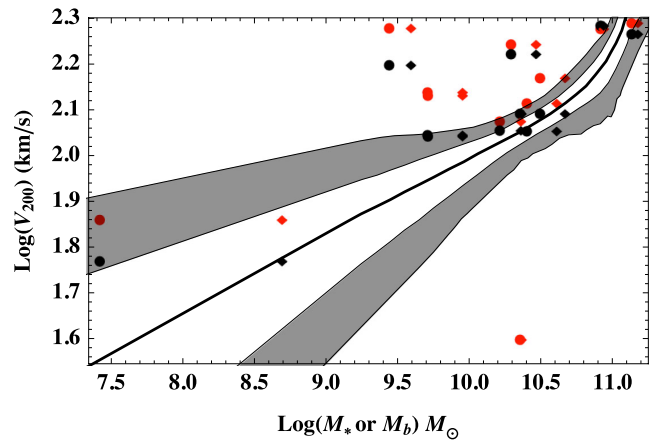


Figure 21. Relationship between the stellar mass and baryonic mass with V_{200} . Black points represent value from the de Blok et al. (2008) NFW halo fits and red points represent the value from our primordial NFW haloes. The circles are plotted against only the stellar mass whereas the diamonds are plotted against the total baryonic mass (stars + gas). The shaded region is the expectation from Reyes et al. (2012) for only the stellar mass relation. The 1σ confidence region in white and the 2σ confidence region shown in grey. The regions have been corrected to reflect the stellar IMF used in this paper.

Taking our own result at face value, $V_p \approx V_{200}$ with substantial scatter (~ 0.2 dex; Fig. 22). We infer similar or somewhat larger V_{200} at a given stellar mass than do Reyes et al. (2012), and a smaller f_v (1.0 rather than 1.3). This in itself is not inconsistent with the OVVR of Reyes et al. (2012) as we have not averaged over the scatter in a similar fashion. Clearly the observed velocity is related to that of the parent dark matter halo, but considerable caution must be exercised in relating one to the other for any given galaxy.

There is a hint that our data follow the same trend with mass as suggested by the bands in Figs 21–23, but there is not enough data to say anything definite. Indeed, the information at low masses from all sources is rather patchy and not obviously trustworthy. We can neither confirm nor refute the trend in f_v inferred from the halo occupation distribution (More et al. 2011) or the Tully–Fisher relation (McGaugh 2012). The NFW halo model rarely fits low-mass galaxies, so it is not obvious that extrapolations to low mass can be meaningful.

² Note that the precise value of the constant in this equation depends on the choice of $\Delta = 200$, the calibration of the BTFR, and mildly on cosmological parameters – see McGaugh (2012).

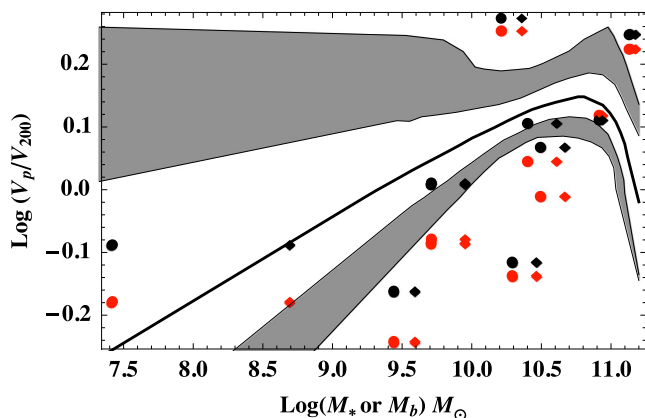


Figure 22. Relationship between the stellar mass and baryonic mass with V_p/V_{200} where V_p is the circular velocity at the radius where the baryonic mass model peaks. This is equivalent to $V_{2.2}$ for purely exponential discs (McGaugh 2005a). Black points represent value from the de Blok et al. (2008) NFW halo fits and red points represent the value from our primordial NFW haloes. The circles are plotted against only the stellar mass whereas the diamonds are plotted against the total baryonic mass (stars+gas). The shaded region is the expectation from Reyes et al. (2012) for only the stellar mass relation. The 1σ confidence region in white and the 2σ confidence region shown in grey. The regions have been corrected to reflect the stellar IMF used in this paper.

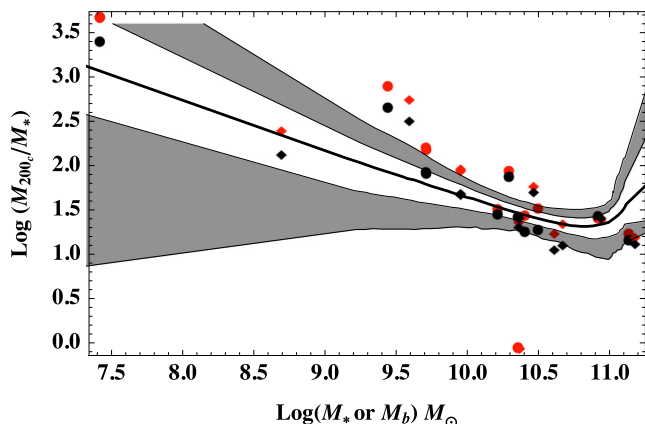


Figure 23. Relationship between the stellar mass and baryonic mass with $M_{200}/(M_*$ or $M_b)$. Black points represent value from the de Blok et al. (2008) NFW halo fits and red points represent the value from our primordial NFW haloes. The circles are plotted against only the stellar mass whereas the diamonds are plotted against the total baryonic mass (stars+gas). The shaded region is the expectation from Reyes et al. (2012) for only the stellar mass relation. The 1σ confidence region in white and the 2σ confidence region shown in grey. The regions have been corrected to reflect the stellar IMF used in this paper.

4 CONCLUSION

We have modelled the primordial haloes of 12 galaxies from the THINGS survey by using Young’s algorithm to exactly calculate adiabatic compressions of dark matter haloes. We find a general trend that concentration and virial velocity of the primordial halo decrease and increase, respectively, when compared to the best-fitting NFW halo of the rotation curve. For the majority of galaxies, we find that the compressed halo is statistically comparable to the regular best-fitting NFW halo and in some cases even better.

The NFW parameters for the primordial haloes fall on and slightly below the $c-V_{200}$ relation predicted by Λ CDM. It appears possible

that adiabatic contraction has dominant effect that reshapes the dark matter haloes of massive spiral galaxies. This does not preclude the influence of other effects, like feedback. Indeed, such a process does appear to be necessary in some galaxies, but not necessarily in all. It is tempting to conclude that feedback becomes progressively more relevant in lower mass galaxies, but there can be exceptions at both high and low mass, so one must be careful not to overgeneralize.

A trend has emerged between the virial velocity of the primordial halo and the stellar/baryonic mass of a galaxy. A similar trend is also present for the concentration of the primordial halo and the galaxy mass, albeit with greater scatter. The relations derived from these trends can be used to estimate the parameters of the primordial halo of observed galaxies without formally computing the compression. A larger sample of galaxies would be useful to better constrain these relations.

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